

16 – more texture

Bump Mapping and Environment Mapping

Basic Algorithm

for each pixel (x_s, y_s)

create a ray R from eye through (x_s, y_s)

for each object O_i in scene

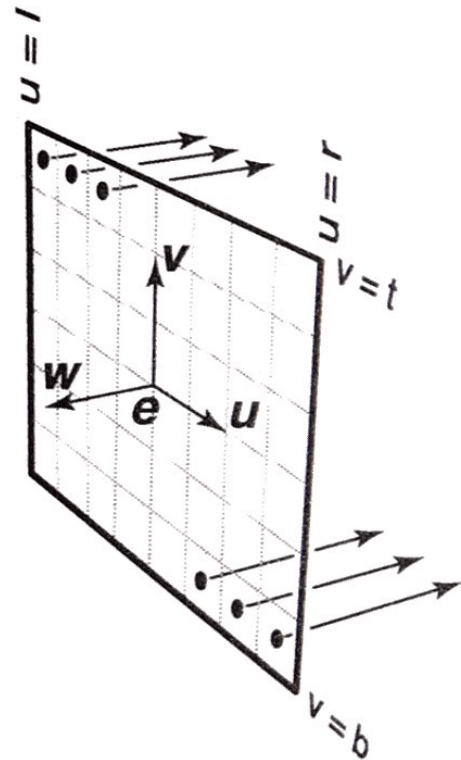
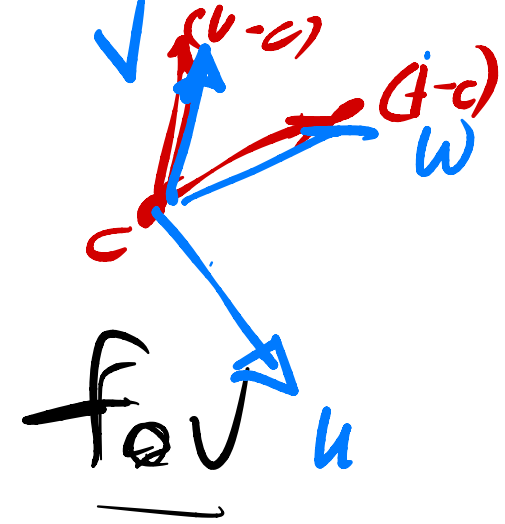
[if R intersects O_i & it's the closest
so far

[record this intersection

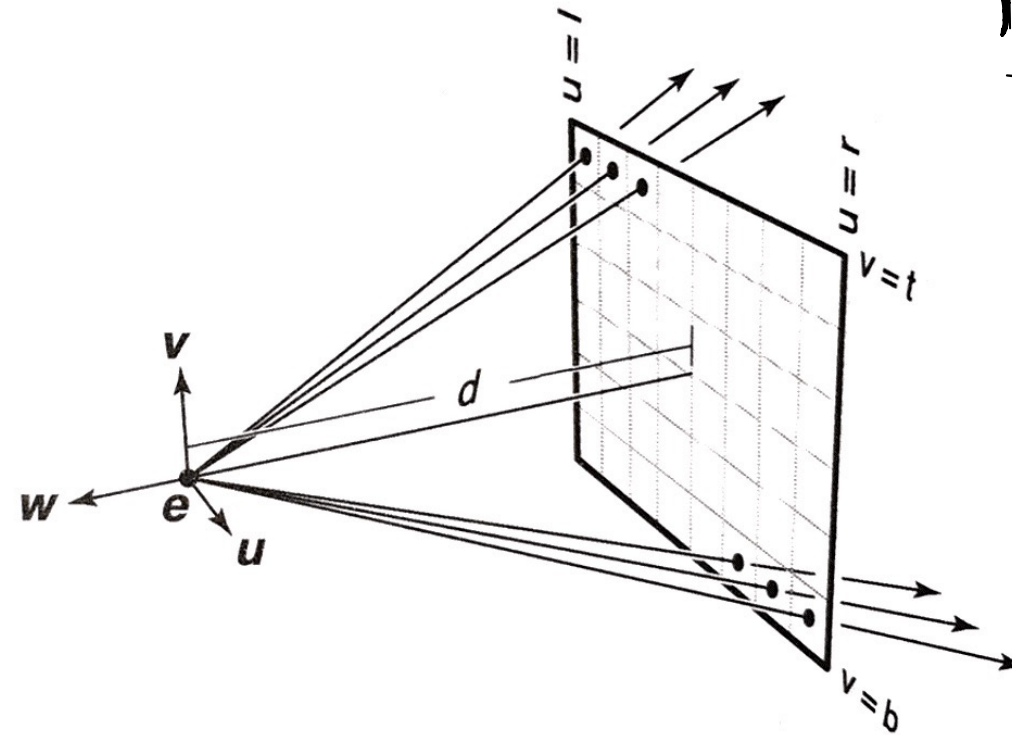
shade pixel based on nearest intersection
(recursively for ref & transmission)

Eye Rays: Depends on Projection (Orthographic, Perspective, Oblique)

c, l, u



Parallel projection
same direction, different origins

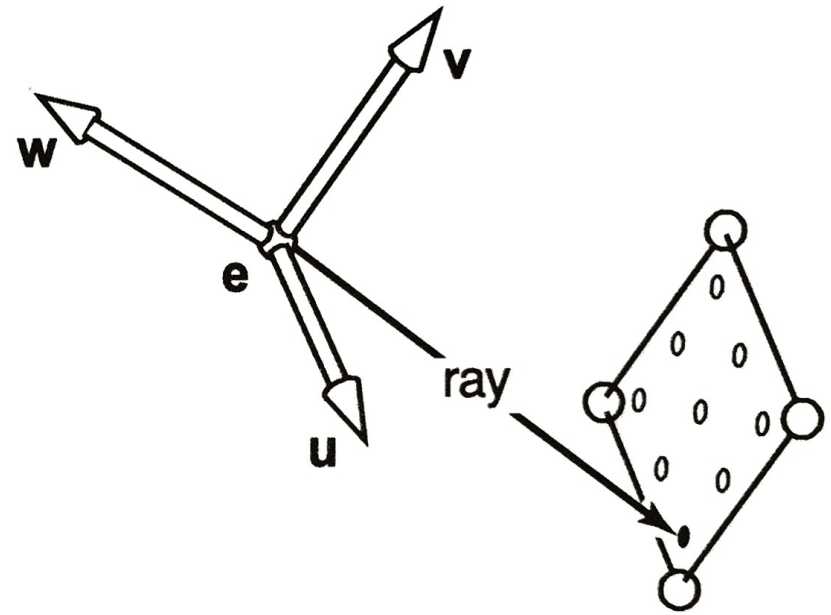
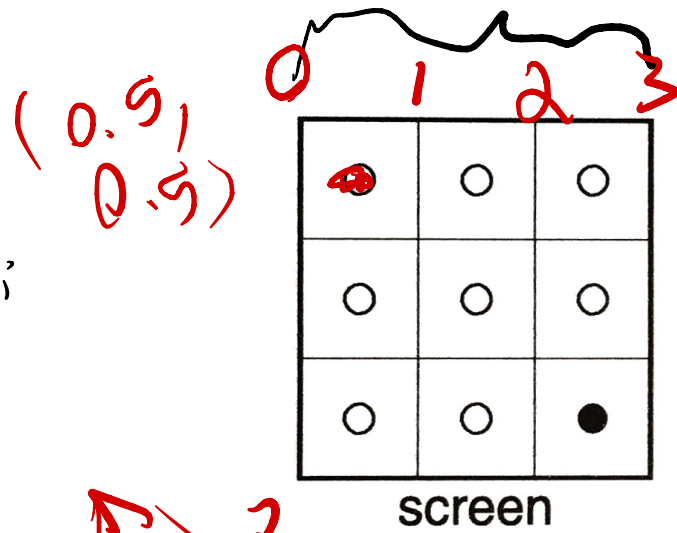


Perspective projection
same origin, different directions

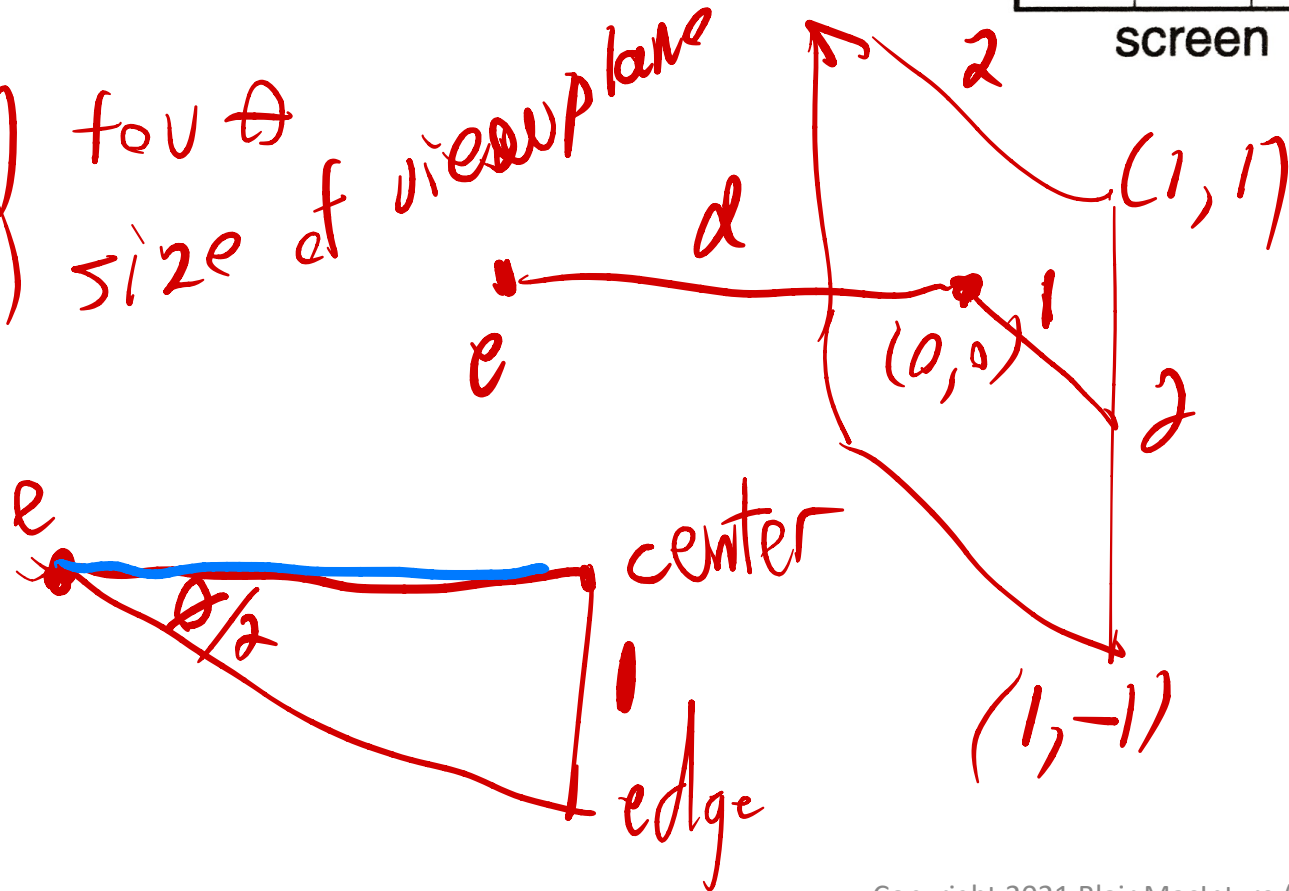
FOV = FOVY

Parametric eq'n:

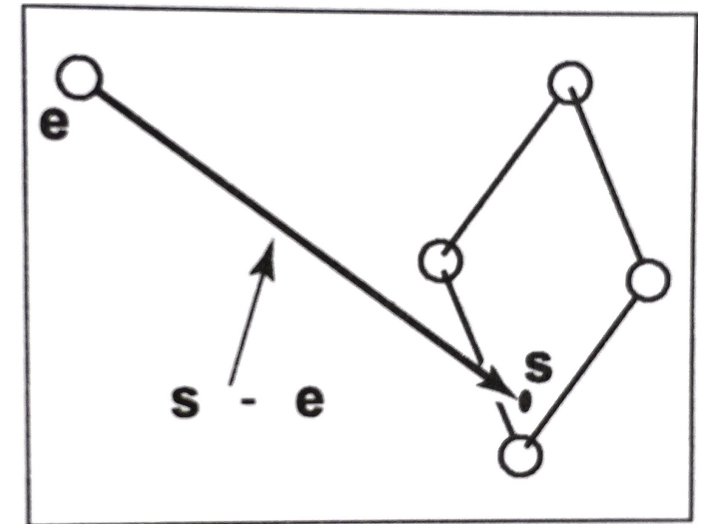
$$p(t) = e + t(s - e)$$



- 1) FOV θ
- 2) size of view plane



$$d = \frac{1}{\tan(\frac{\theta}{2})}$$



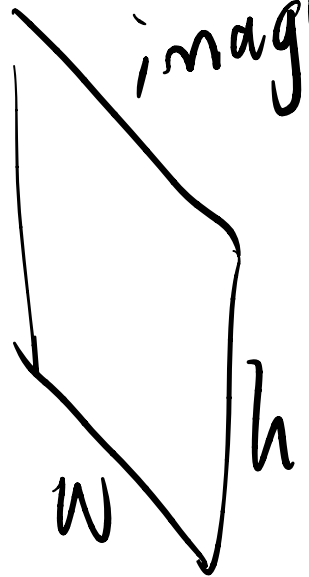
$$u_s = -1 + \frac{2i}{h}$$

$$v_s = -1 + \frac{2i^w}{h}$$

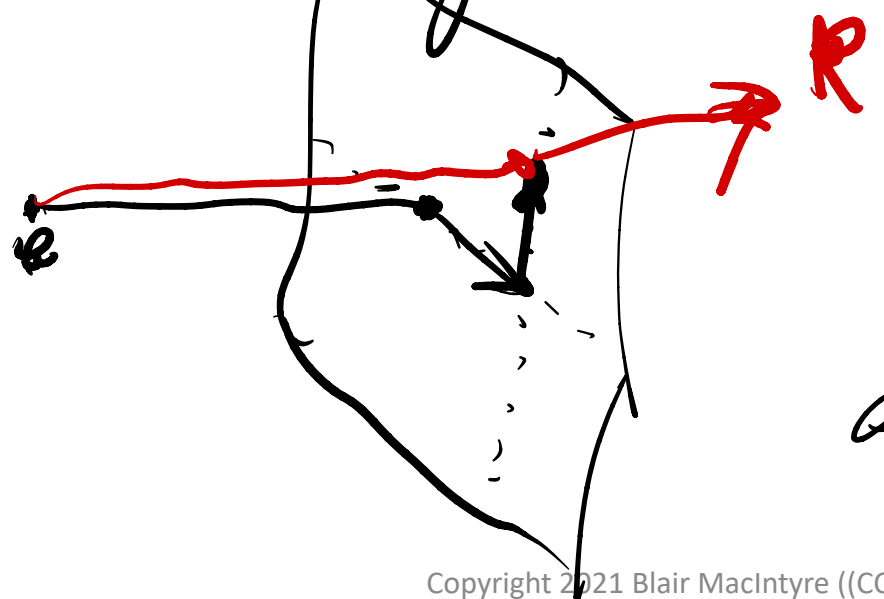
image

u & v
-1 radii range

u
v
w



ray direction = $\frac{s - e}{|s - e|}$



$$= -dw + u_s u + v_s v$$

origin = e

for

Bump Mapping

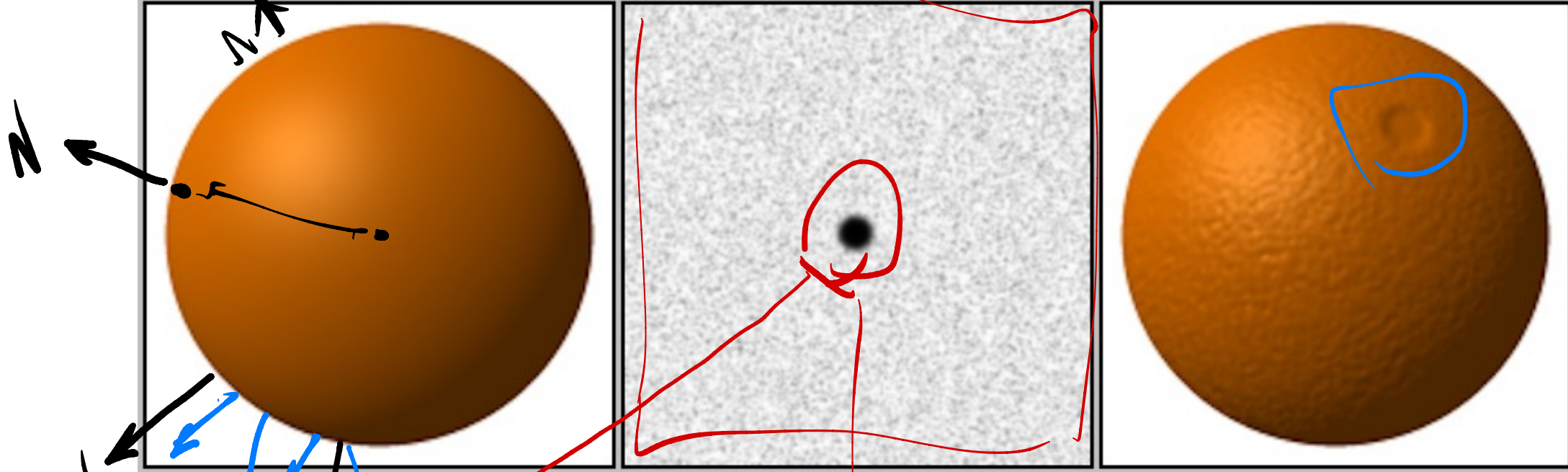


From this

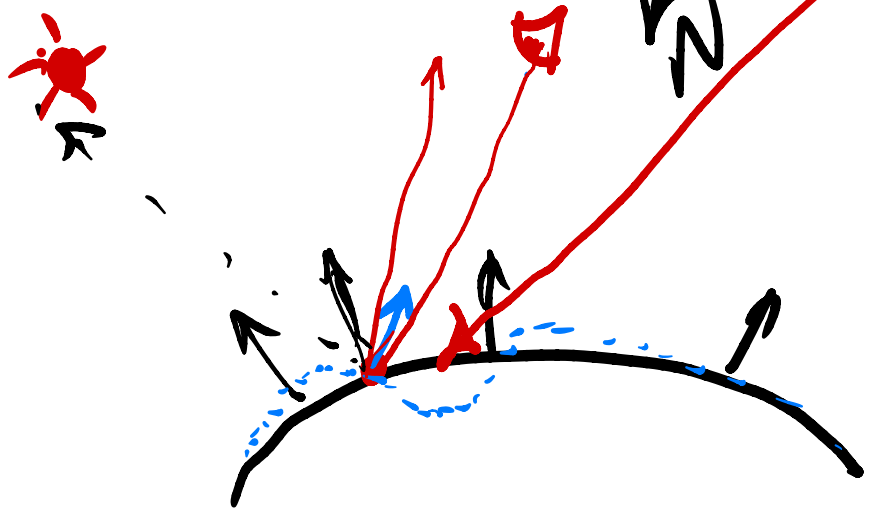
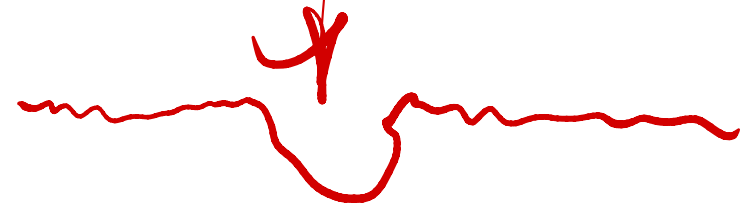


to this

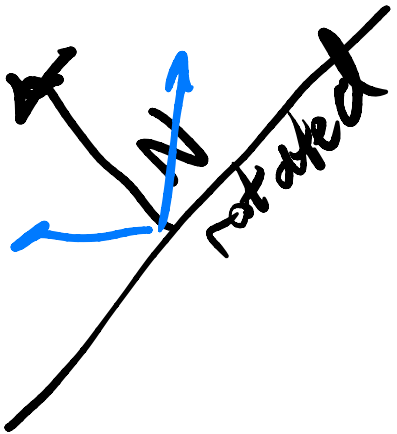
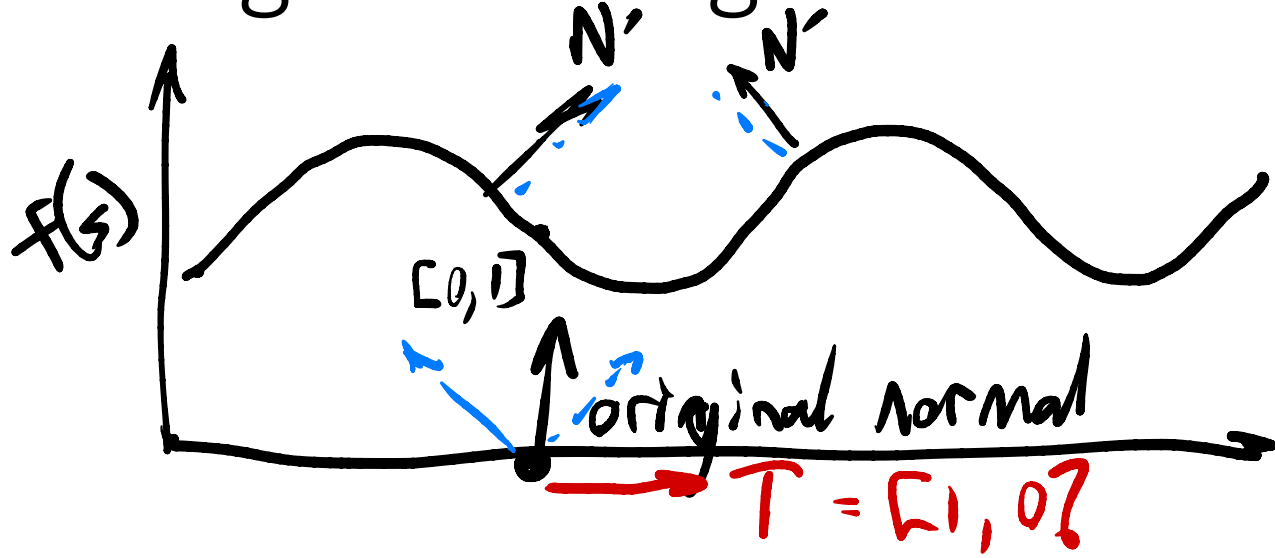




Bump map
grayscale texture
value encodes height



High level algorithm



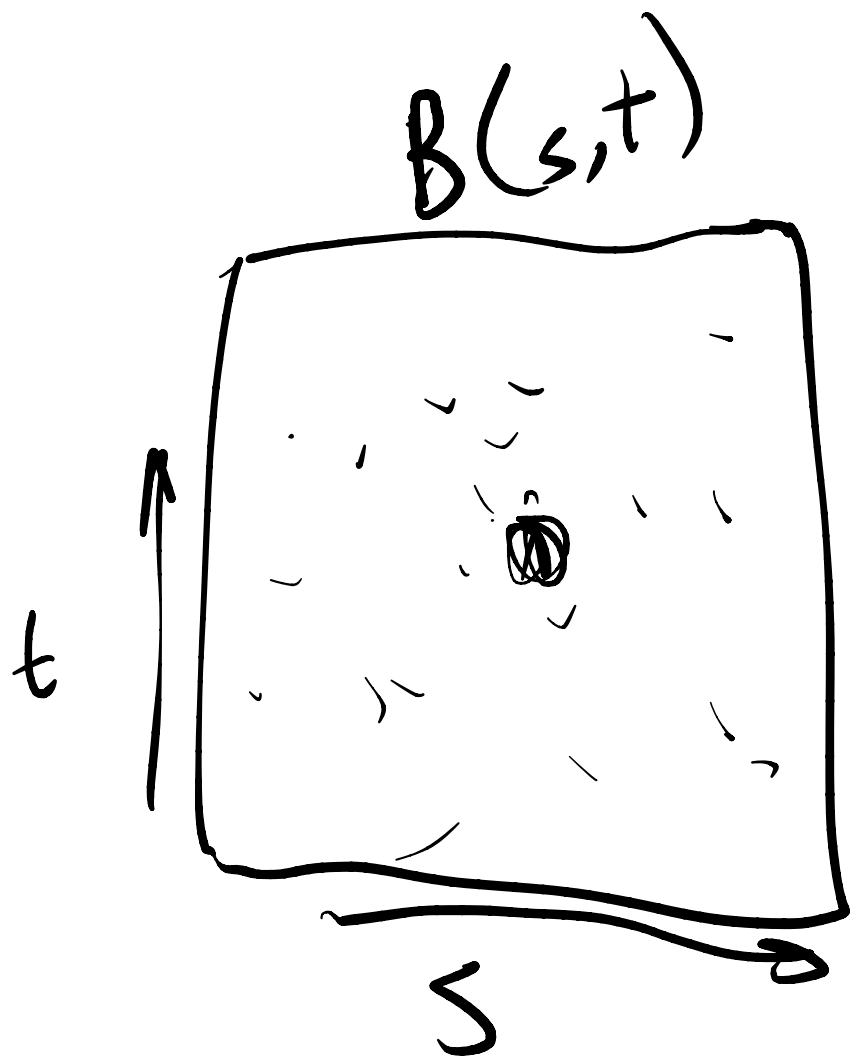
$$N = N - f(s) [1, 0]$$

$$f(s) = [f_1 \dots f_n]$$

$$0 \dots 255 \rightarrow -1 \dots 1$$



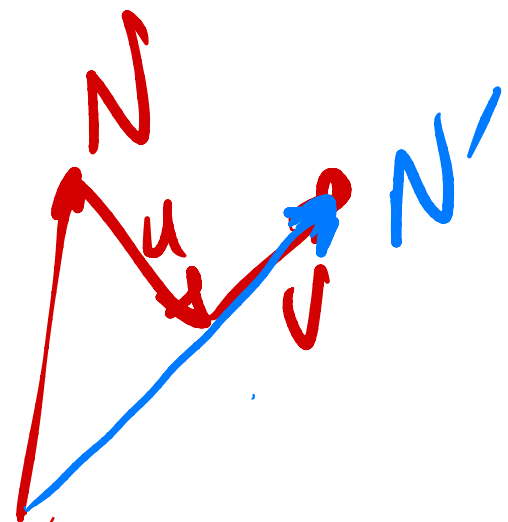
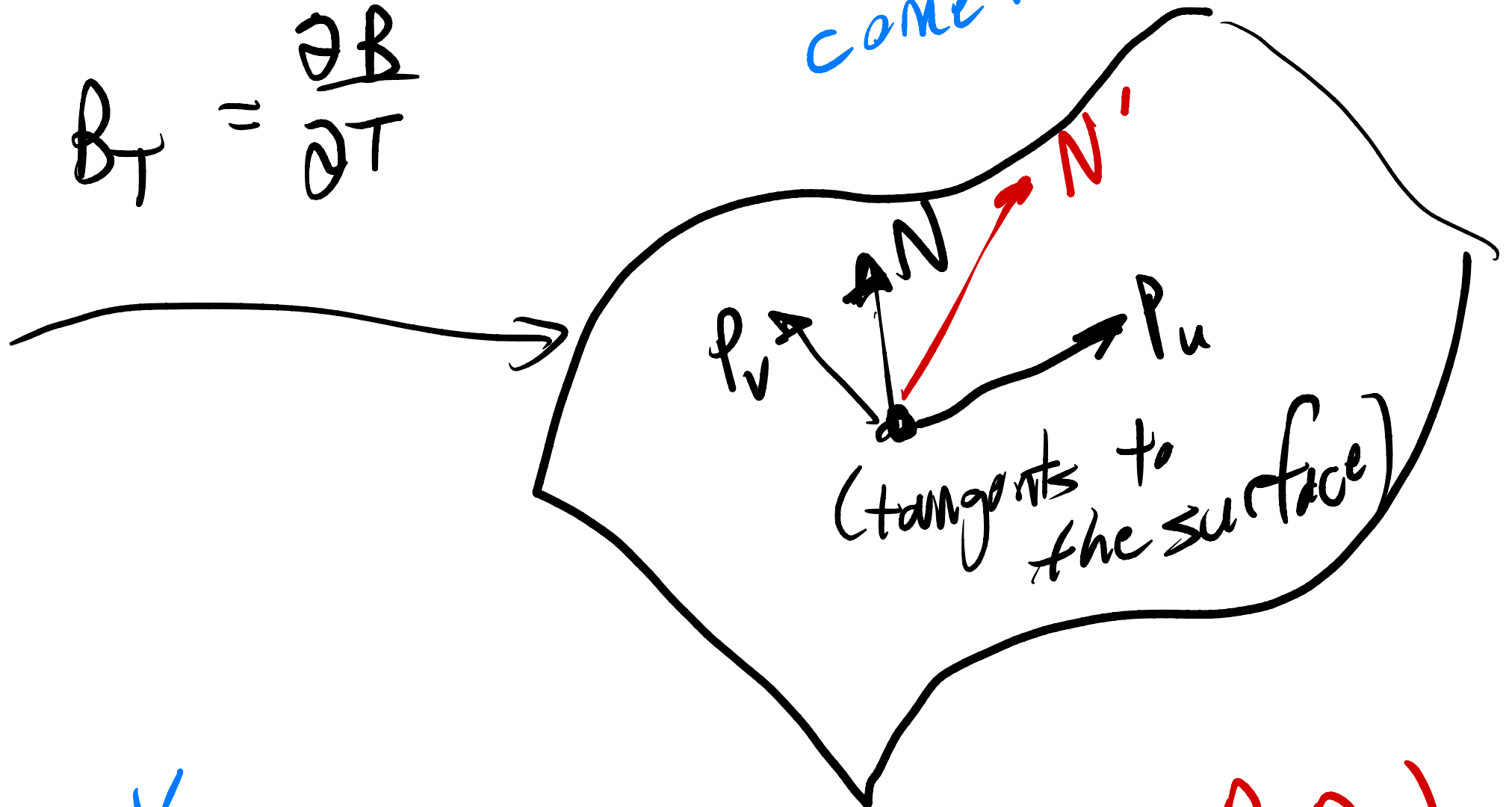
texture does not encode slope



$$B_s = \frac{\partial B}{\partial s}$$

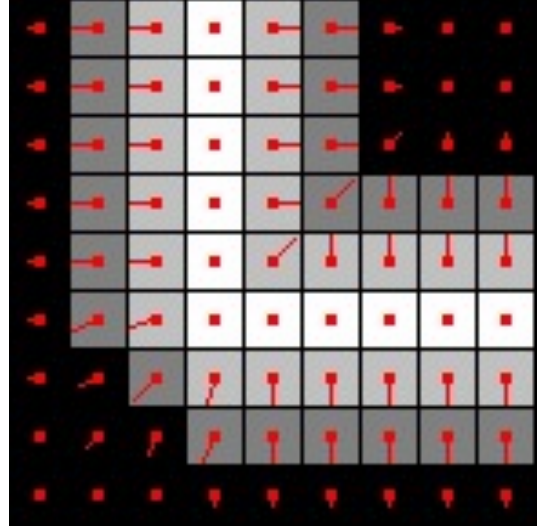
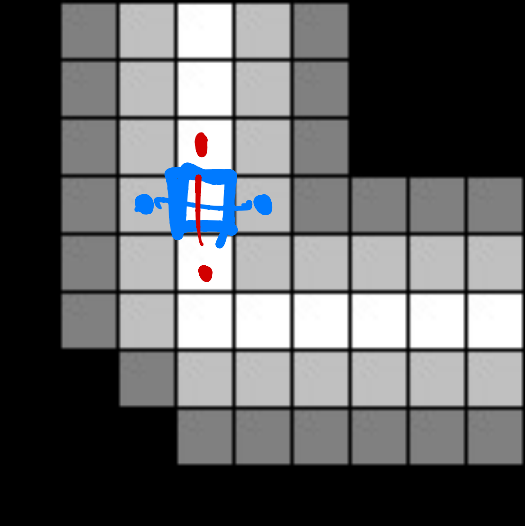
$$B_t = \frac{\partial B}{\partial t}$$

where do P_v & P_u ... ?
 come from



$$N = N' - (B_s P_u + B_t P_v)$$

slopes $(-1 \dots 1)$



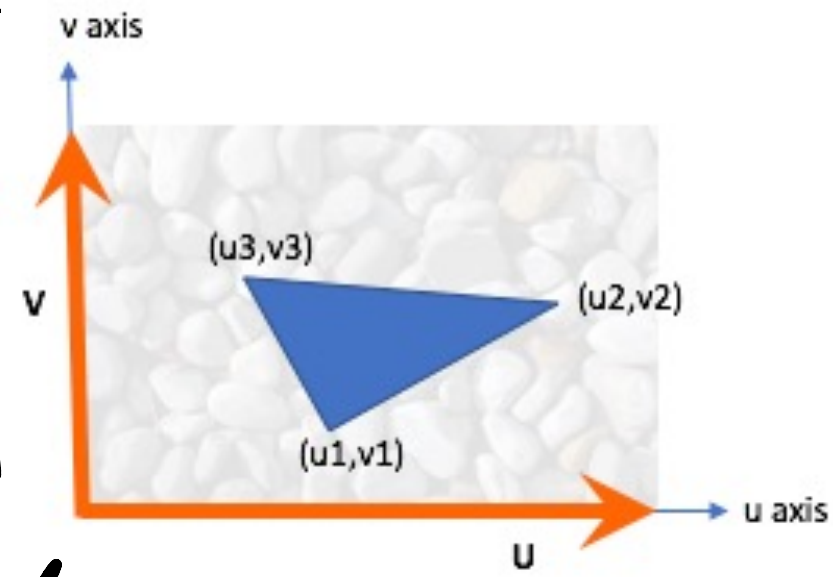
For Triangles

$x_gradient = pixel(x-1, y) - pixel(x+1, y)$
 $y_gradient = pixel(x, y-1) - pixel(x, y+1)$

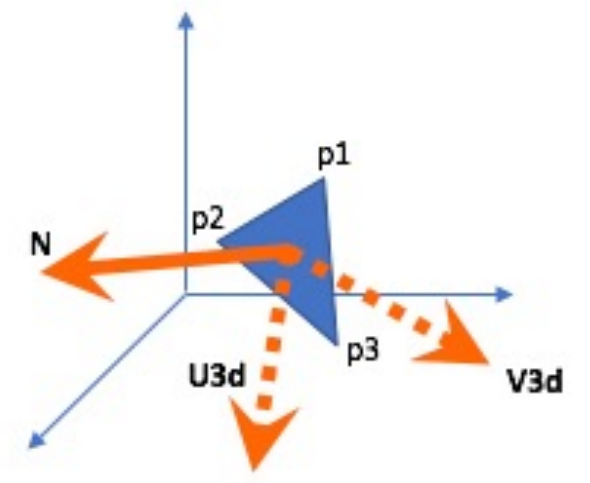
Where do we get B_s & B_t ?

Where do P_u & P_v come from?

want a basis vectors that align with u & v in the texture



A triangle's texture coordinates.



3D object space.

https://csawesome.runestone.academy/runestone/books/published/learnwebgl2/11_surface_properties/10_bump_maps.html

also use Norm Map
in vertex shader

bump map

Color

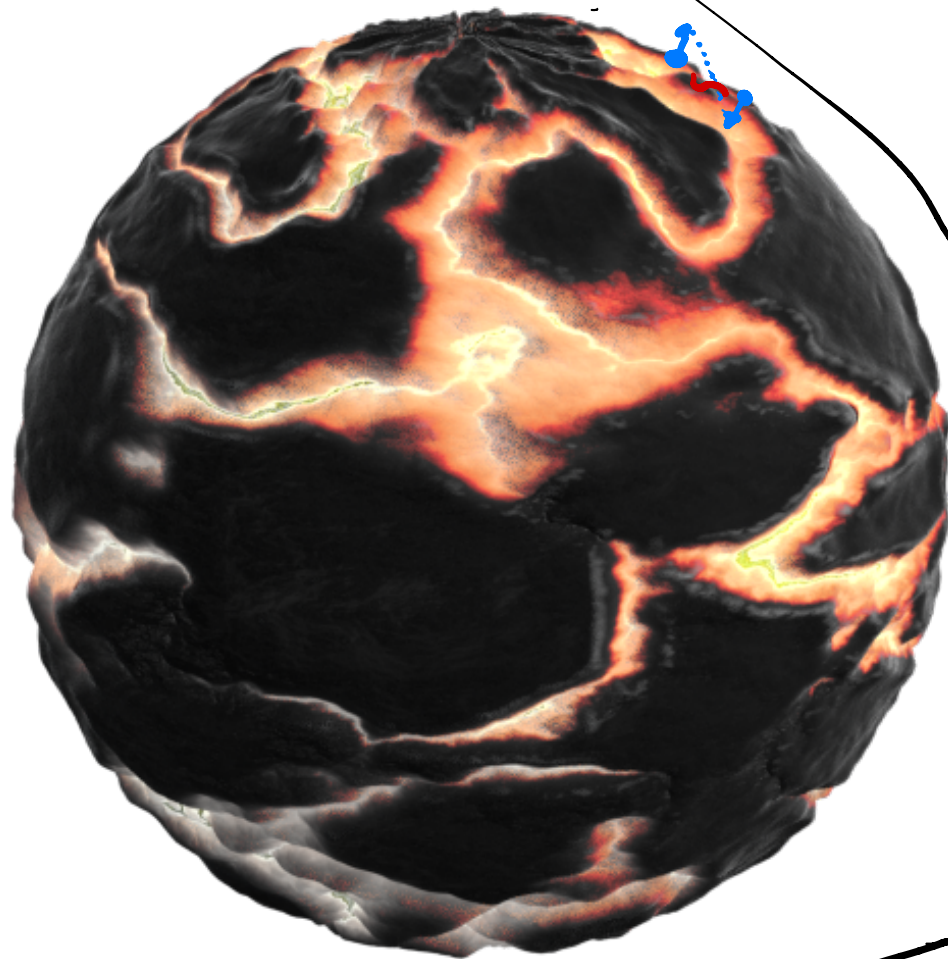


0...255

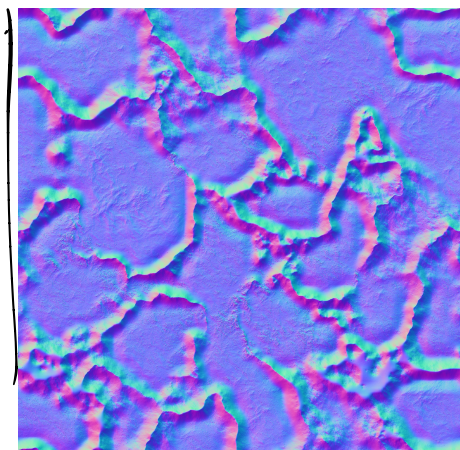
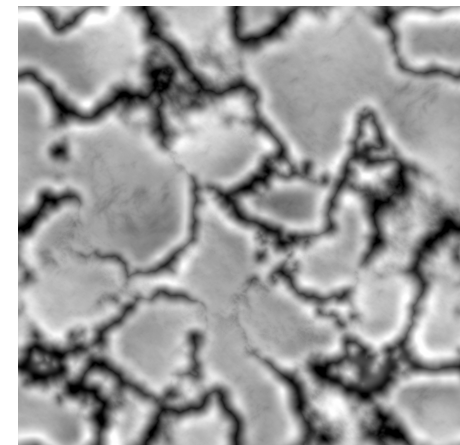
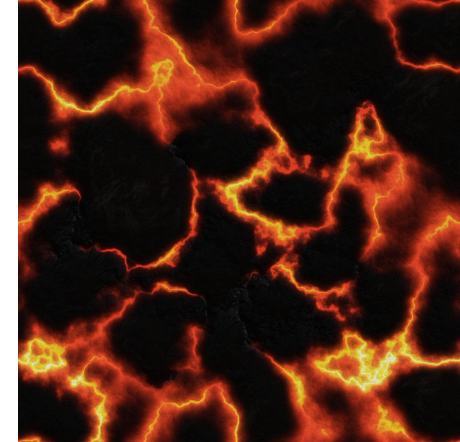
↑ ↓
-1...1 for x, y

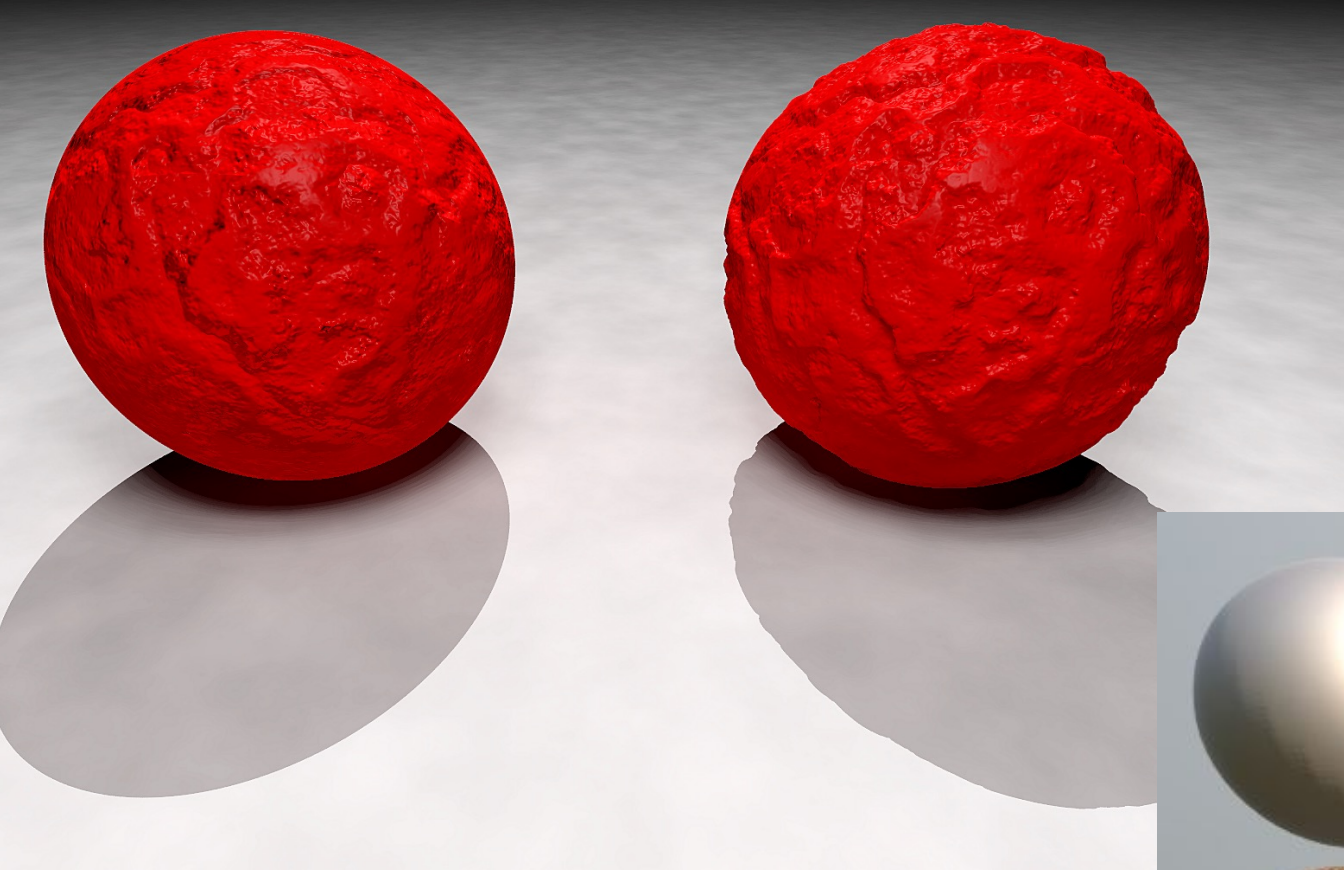
RGB of the normal
is the normal

"(x, y, 1)" → (x, y, z)



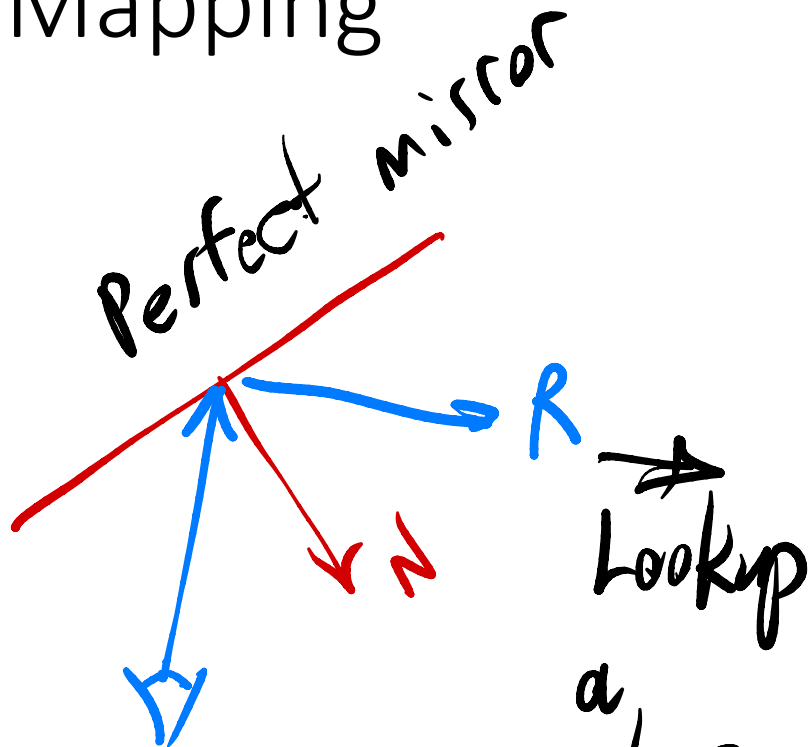
Normal Map





<https://spiderlili.com/2020/03/01/tech-art-tips-tricks-all-about-displacement-normal-bump-maps/>

Environment Mapping



<https://www.youtube.com/watch?app=desktop&v=xLPRHNiXE6w>

image!
of background

No
self reflection!

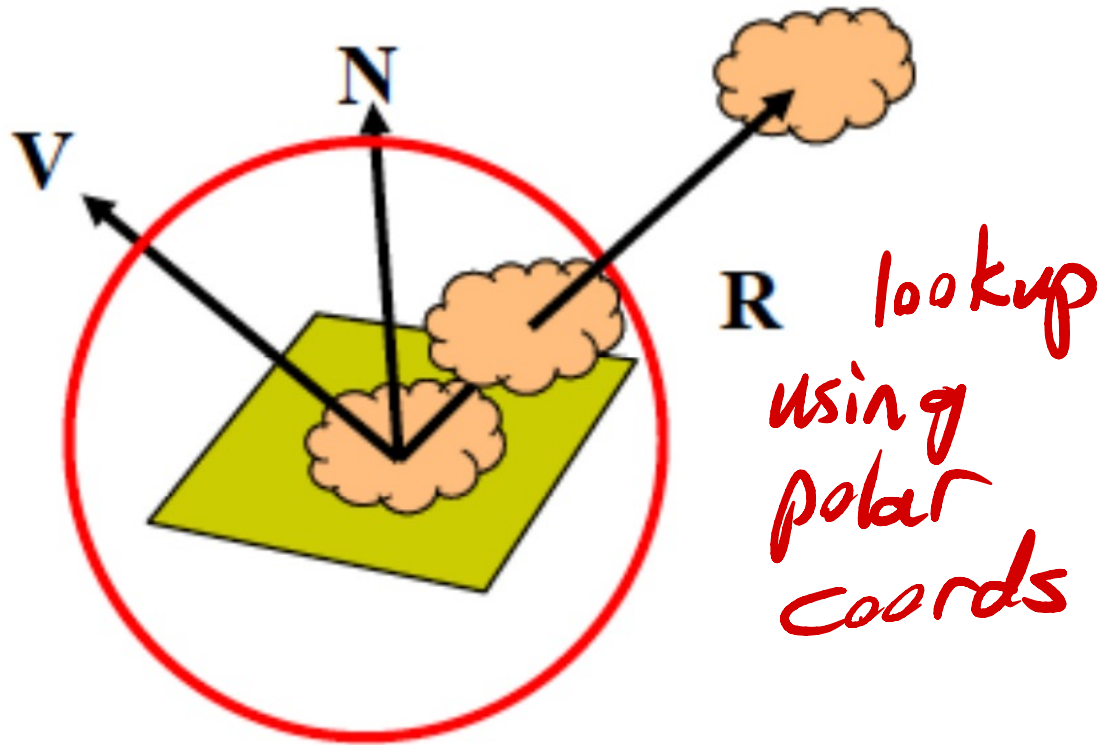
Algorithm

- 1) calculate R (vector) from $N \wedge V$
 - 2) Use R to look up color in env map.
- Texture lookup

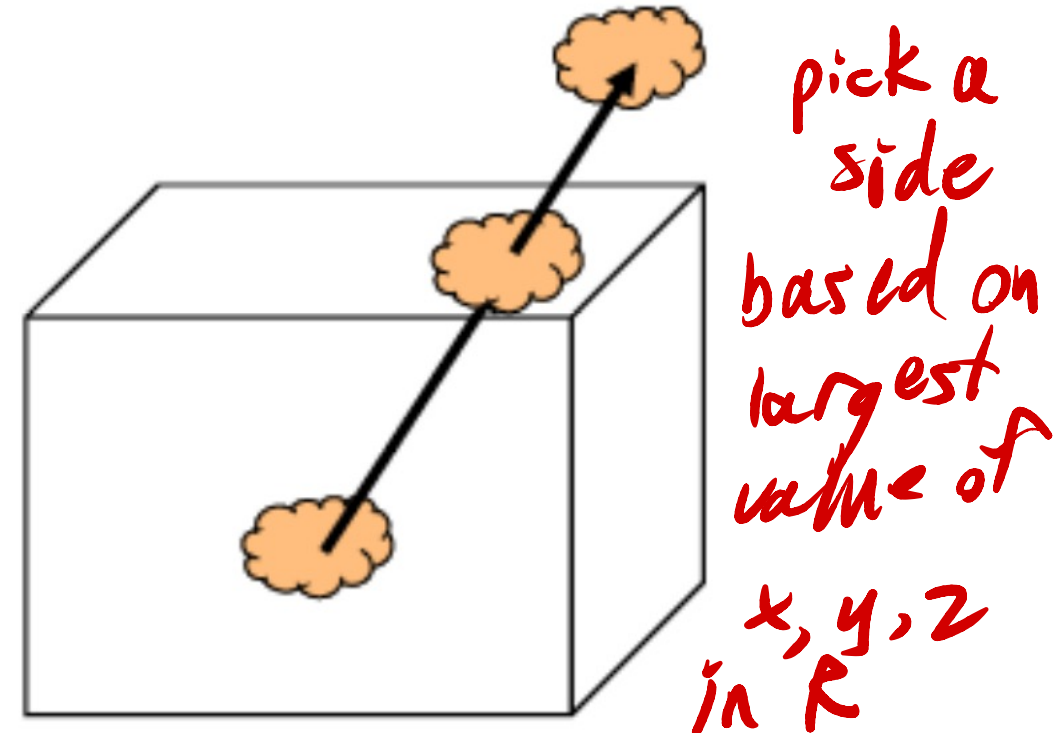
what are (u, v) ← texture coordinates

Two kinds of environment maps

a) Sphere around object (sphere map)



b) Cube around object (cube map)



<https://courses.engr.illinois.edu/cs418/fa2017/418-Lecture%2027%20-%20Environment%20Mapping.pdf>

Sphere maps

top & bottom are a single point



<https://aerotwist.com/tutorials/create-your-own-environment-maps/>

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Cube Map



we can generate these:
render scene
6 times along
each \pm axis

